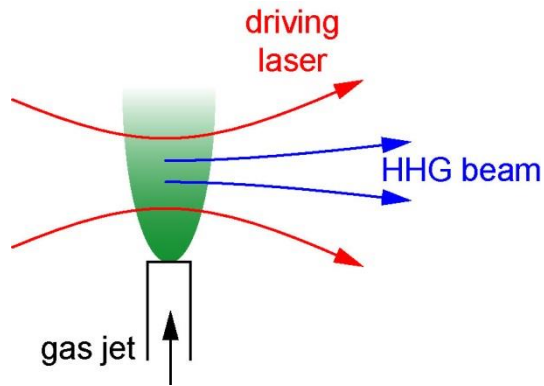


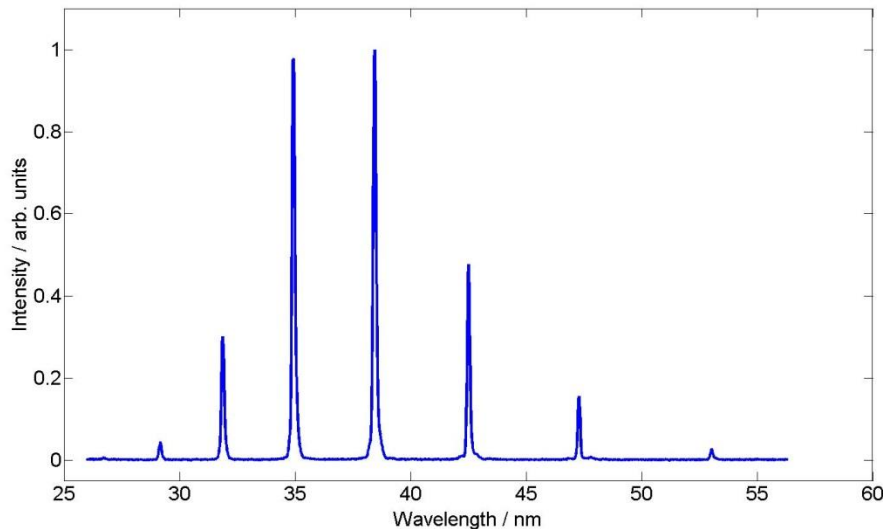
# A tunable source of quasi-phase-matched coherent EUV radiation

Kevin O’Keeffe, David Lloyd, Simon Hooker

# High harmonic generation



- Experimentally straight forward
- Focus ~ 1 mJ, 20-50 fs pulses into gas jet
- Peak intensity  $10^{14} - 10^{15} \text{ W cm}^{-2}$



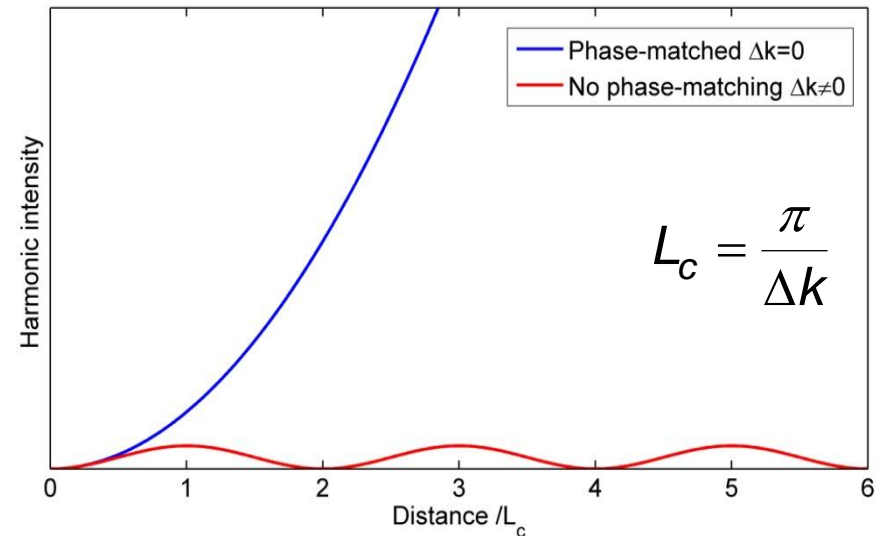
- HHG beam is coherent
- Odd harmonics with order  $q$  up to few hundred
- There is a well-defined cut-off frequency

$$\hbar\omega_{\text{cut-off}} = E_I + \beta I \lambda_0^2$$

# Quasi-phase-matching

- HHG; coherent photons in excess of 1keV
- As in any nonlinear process, efficient harmonic generation requires

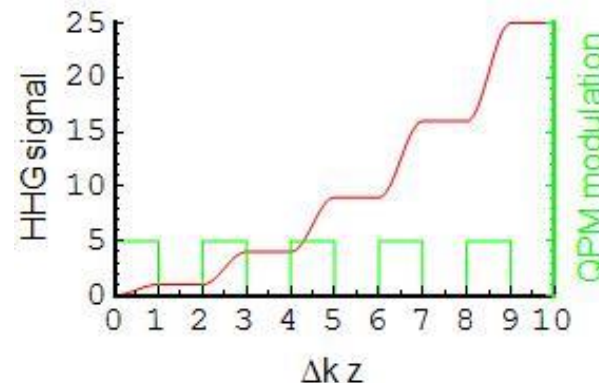
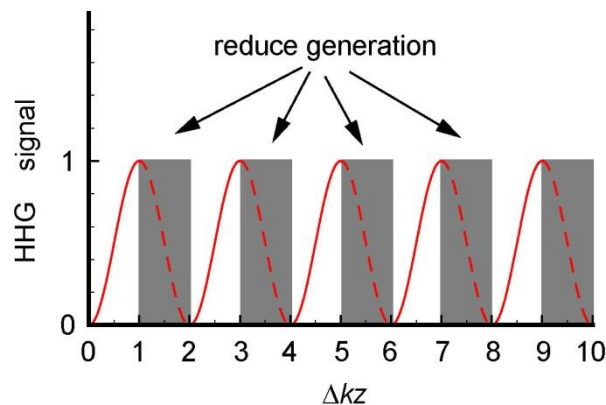
$$\Delta k = qk_{\omega 0} - k_{q\omega 0} = 0$$



## Quasi-phase matching

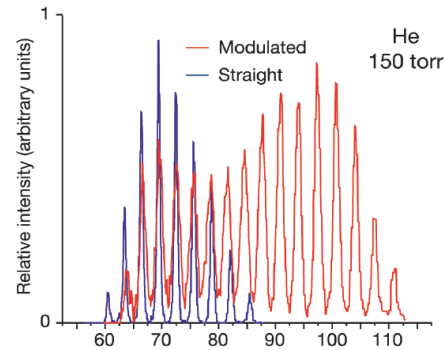
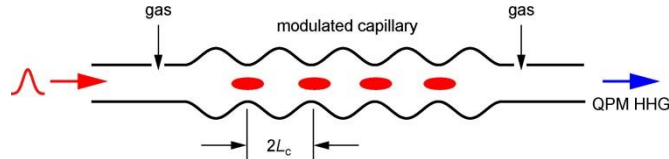
Modulate harmonic generation with period  $L = 2mL_c$   $m = 1, 2, 3, \dots$

Harmonic output increases as  $N^2$ , where  $N$  is number of coherence lengths



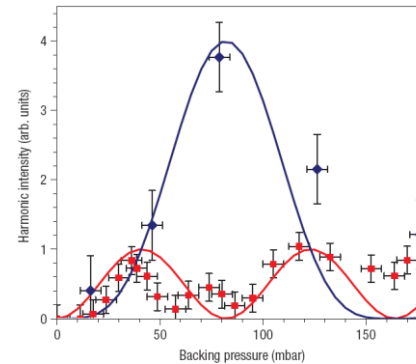
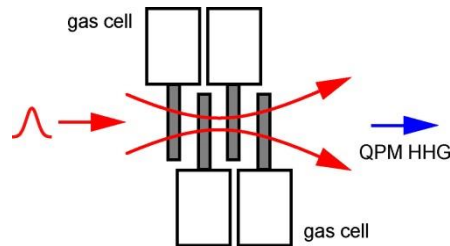
# HHG QPM schemes

- Intensity modulation



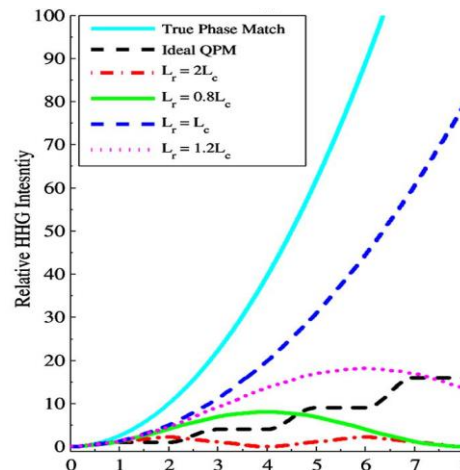
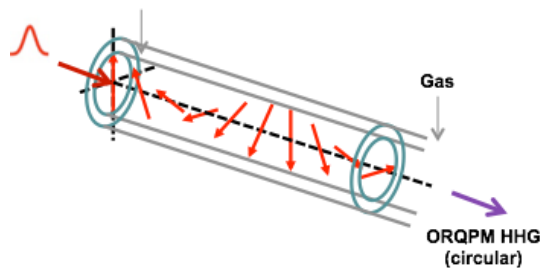
Paul et al. *Nature* **421** 51, (2003)

- Density modulation



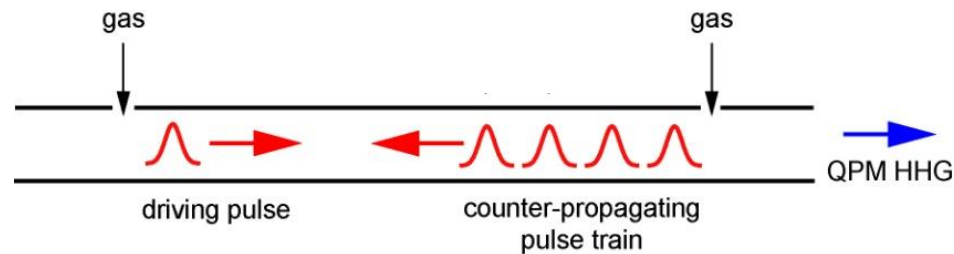
Seres et al. *Nature Physics* **3** 878, (2007)

- Polarization modulation



Liu et al. *Opt. Letts.* **37** 2415, (2012)

# Pulse train QPM



- HHG is suppressed in regions where the driving pulse overlaps with a counter-propagating pulse.
- QPM can be achieved by matching the pulse width and separation to the coherence length

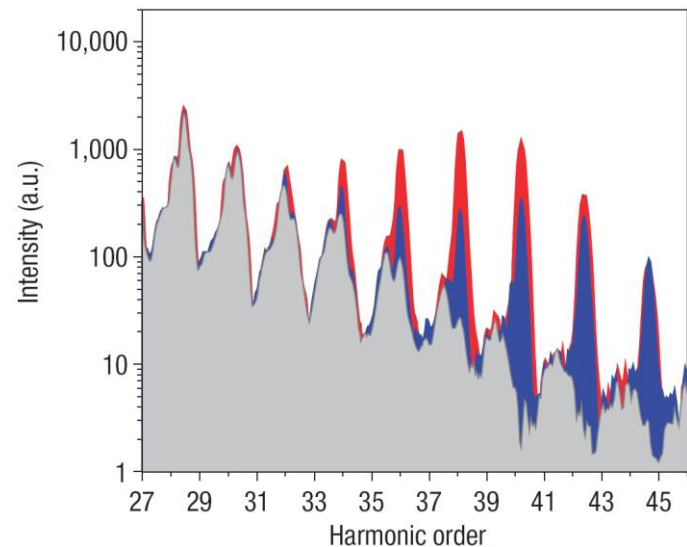
## Experimental conditions

**Capillary:** 6 cm

**Gas:** Ar, 7 Torr

**Pulse train:** 3 pulses, 0.1 mJ

Zhang et al. *Nature Physics*  
3 275 (2007)



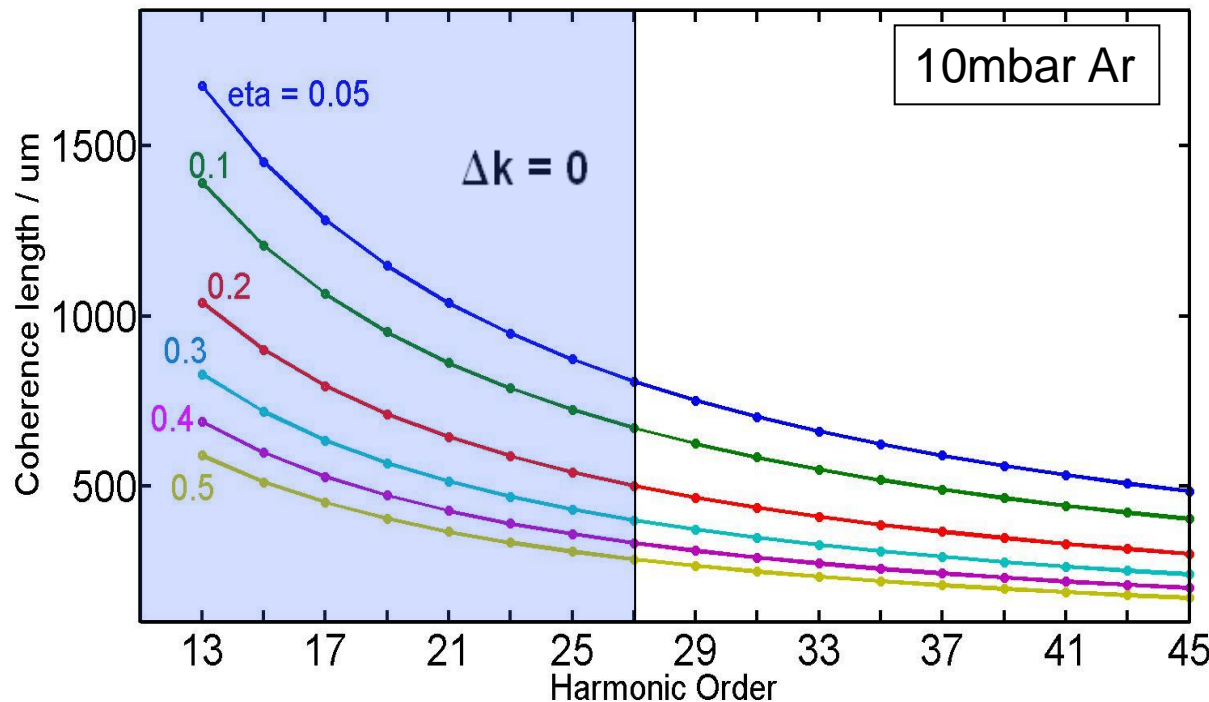
# Matching pulses to coherence lengths

$$\Delta k = \Delta k_{\text{plasma}} + \Delta k_{\text{neutral}} + \Delta k_{\text{waveguide}}$$

$$= -\eta N_a r_e q \lambda_0 + \frac{2\pi q}{\lambda_0} [n(\lambda_0) - n(\lambda_0 / q)] (1 - \eta) \frac{P}{P_{\text{atm}}} - \frac{u_{n,m}^2 q \lambda_0}{4\pi a^2}$$

degree of  
ionization

pressure

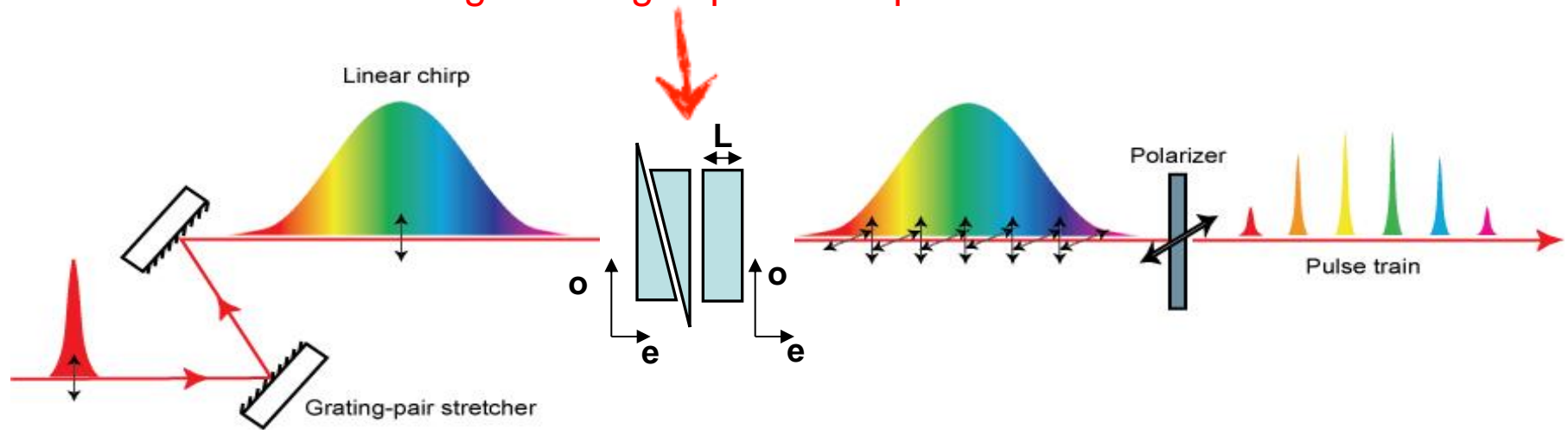


Ideal pulse trains:

- High energy
- High contrast
- Large number of pulses
- Easily tunable

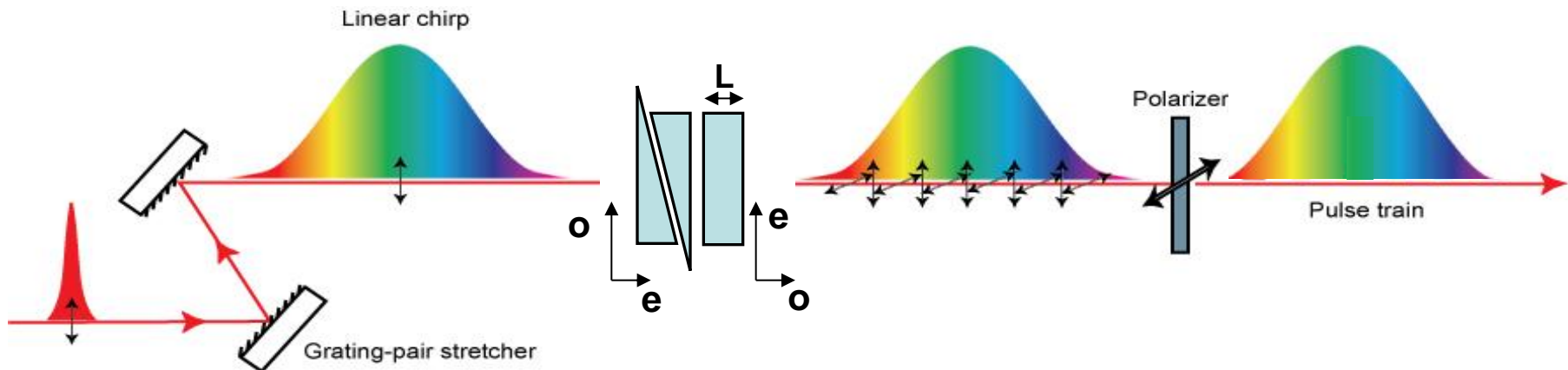
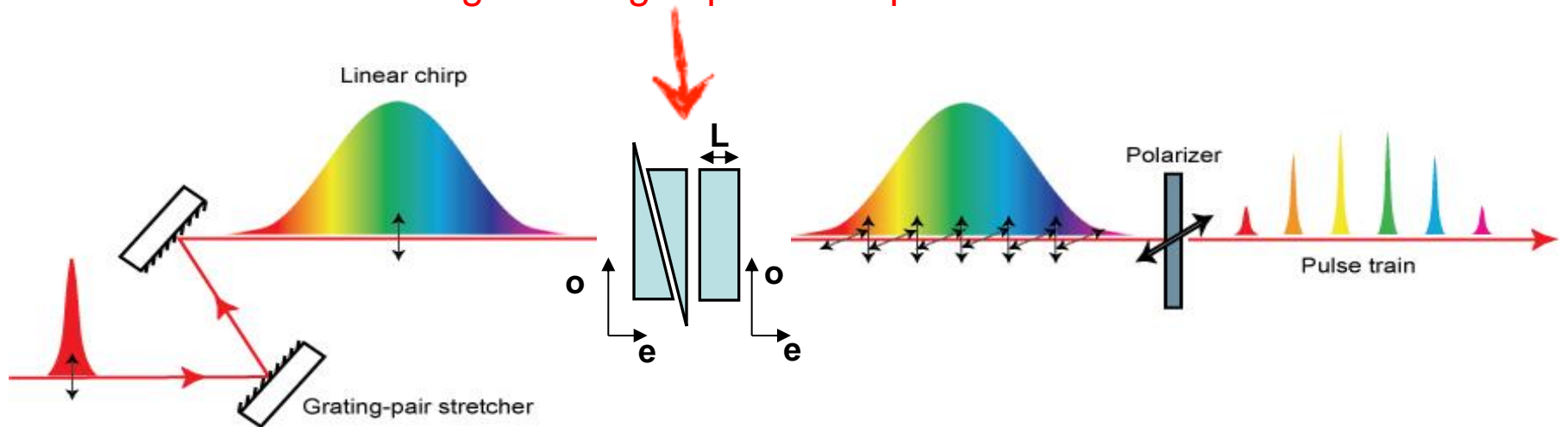
# Tunable pulsetrains

Birefringent wedges plus waveplate



# Tunable pulsetrains

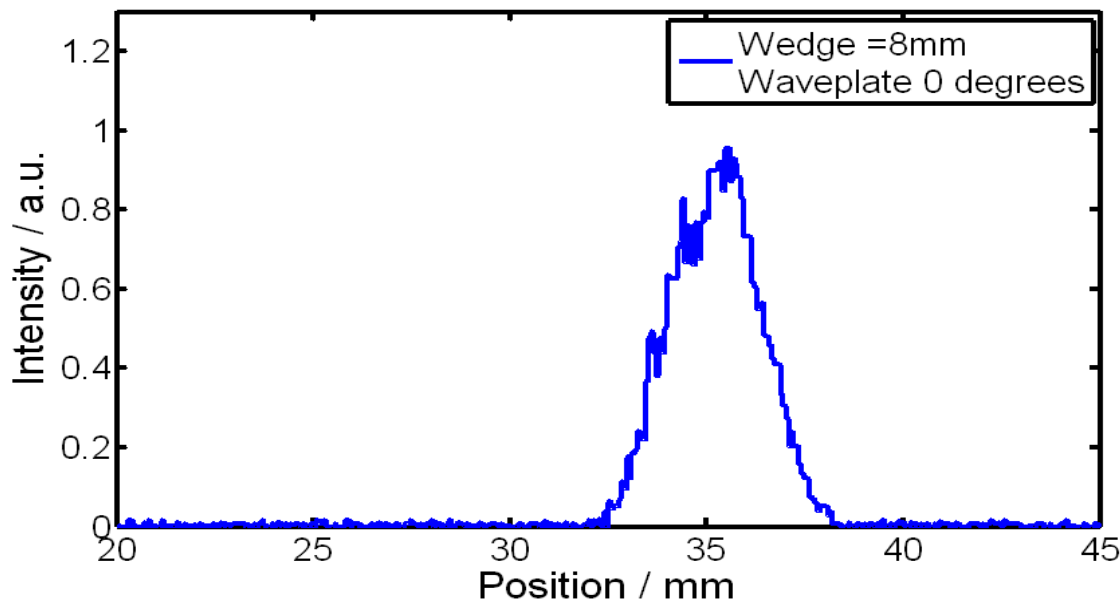
Birefringent wedges plus waveplate



Vary effective thickness from 0 to  $2L$



# Tunable pulsetrains



Cross-correlations of pulsetrain

830 lines/mm grating

14cm grating-retro separation

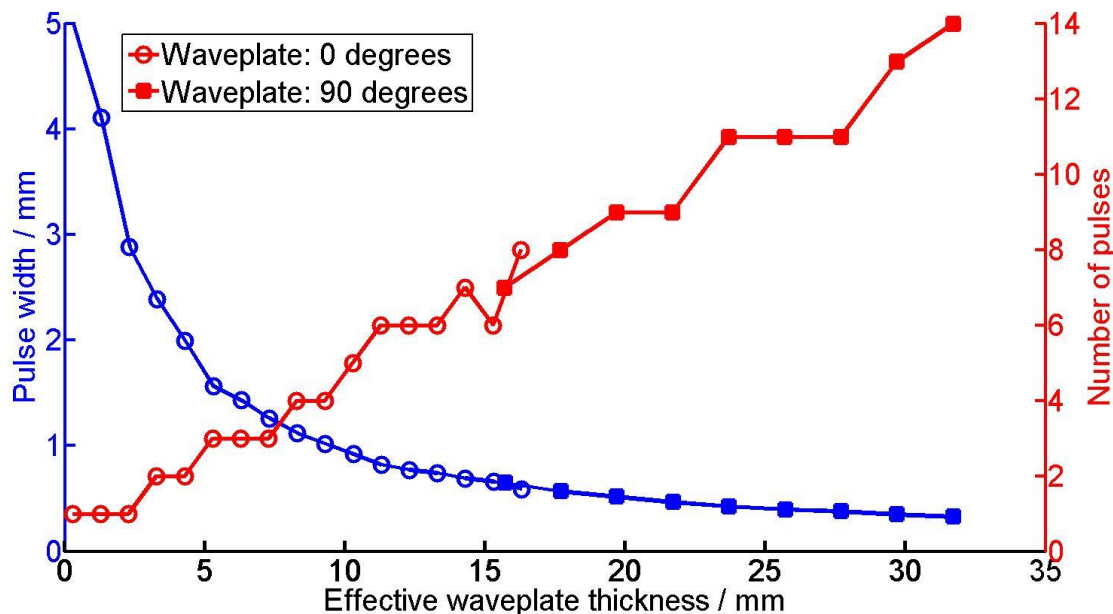
80% in first order

Waveplate: 8mm quartz

Wedges: 1 – 15mm quartz

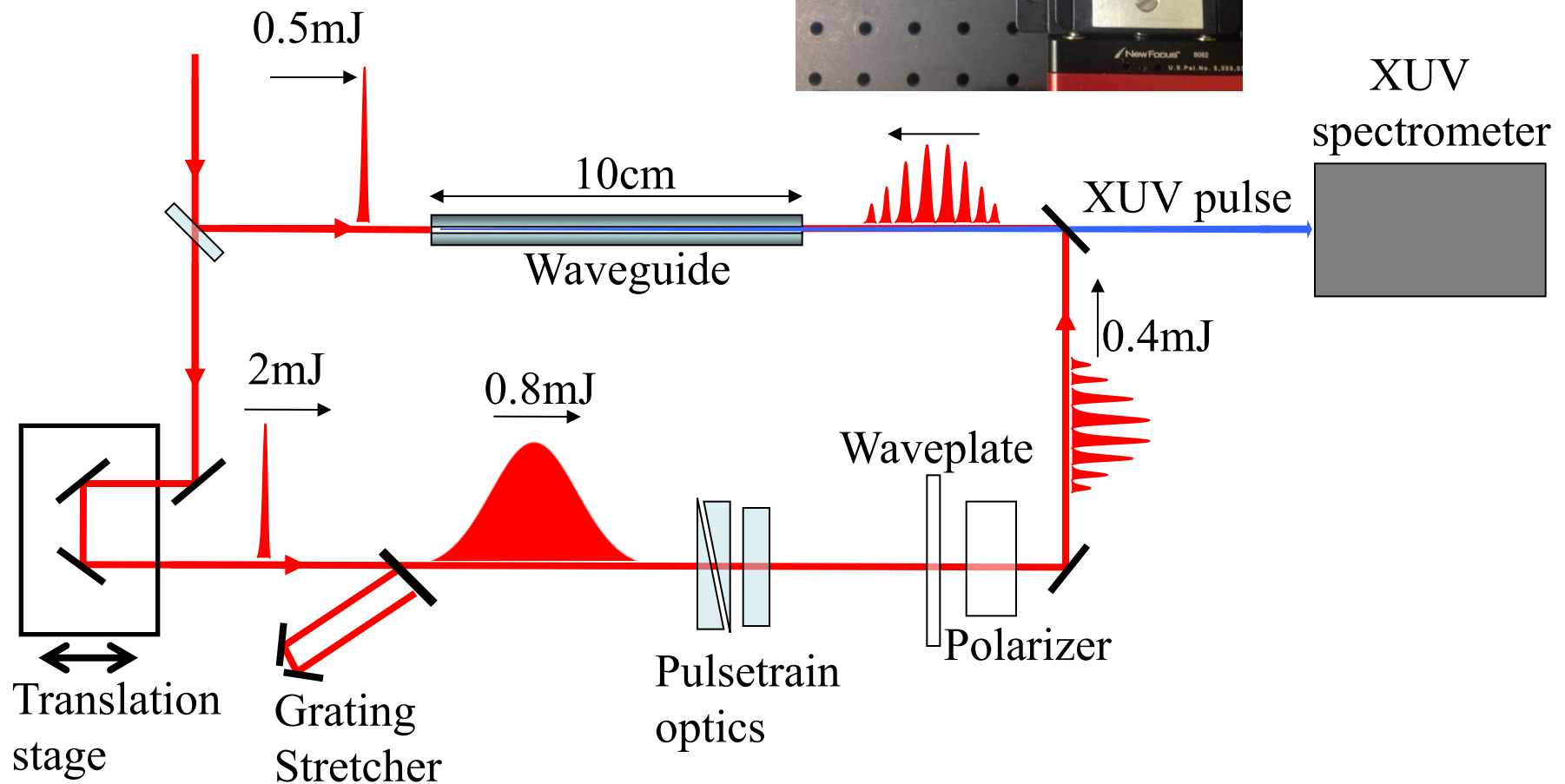
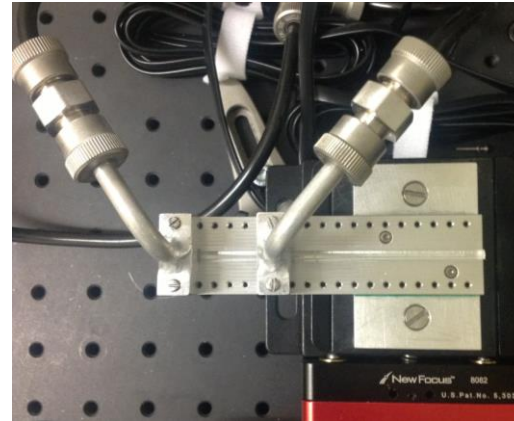
Pulse width  $\sim 1/L$

Total stretch approx. constant

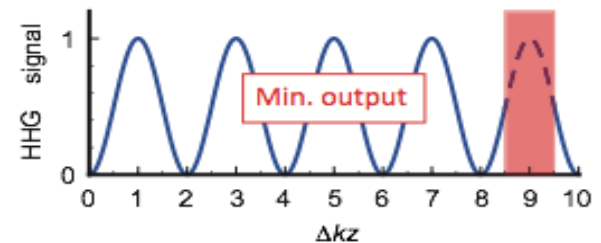
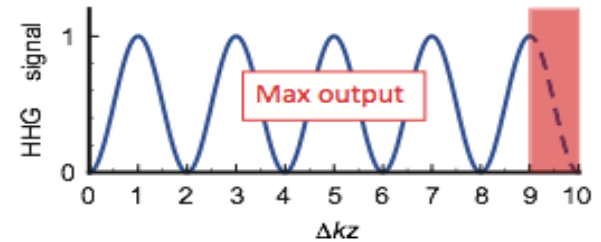
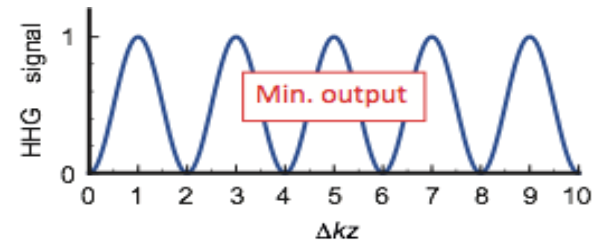
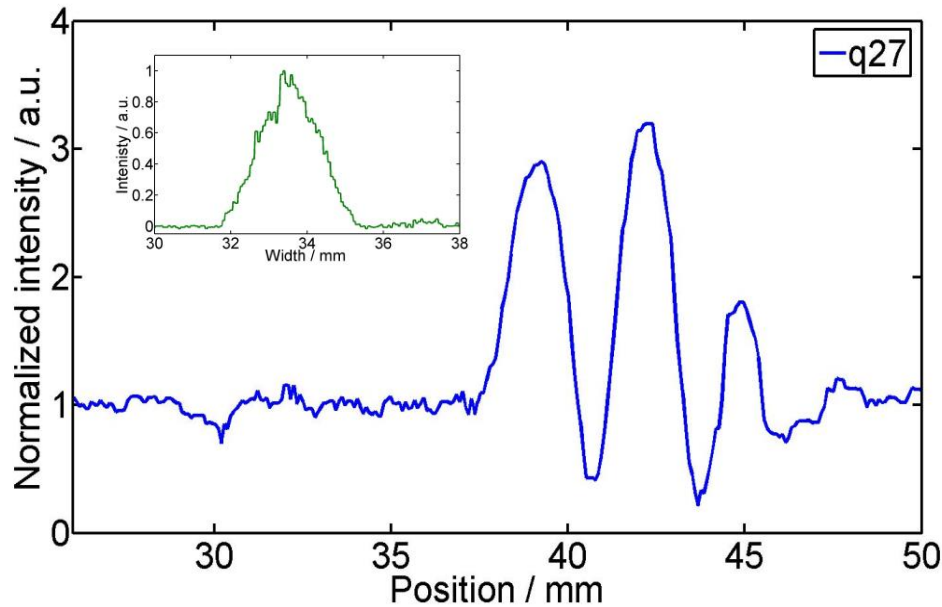


# Pulsetrain experiment

**Laser:** 35fs, 1kHz  
**Driver pulse:** 0.5mJ  
**CP pulse:** 2mJ  
**Gas:** 14mbar Ar

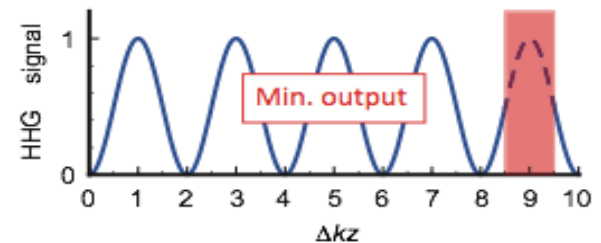
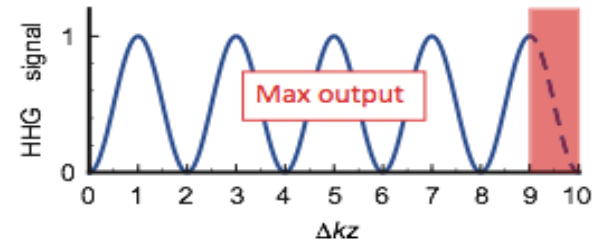
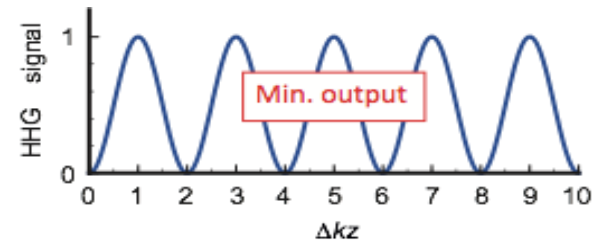
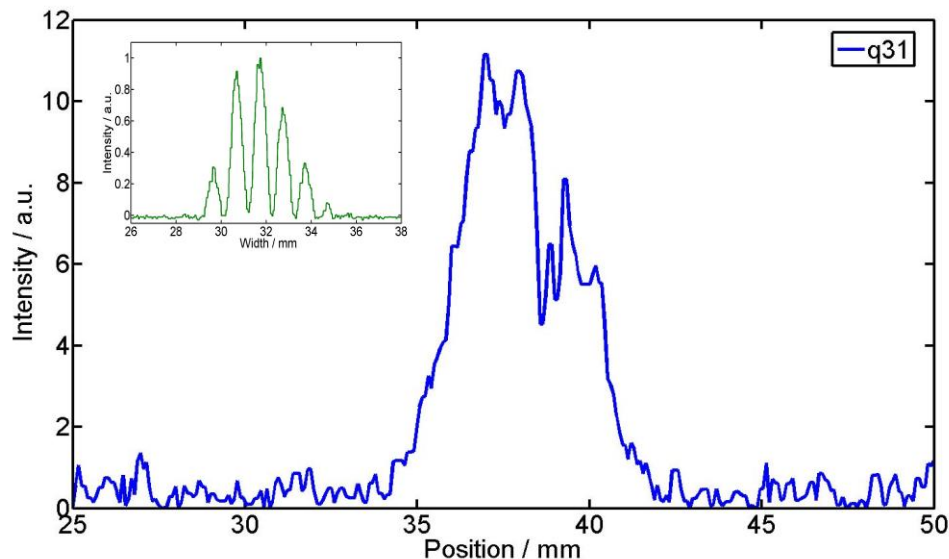
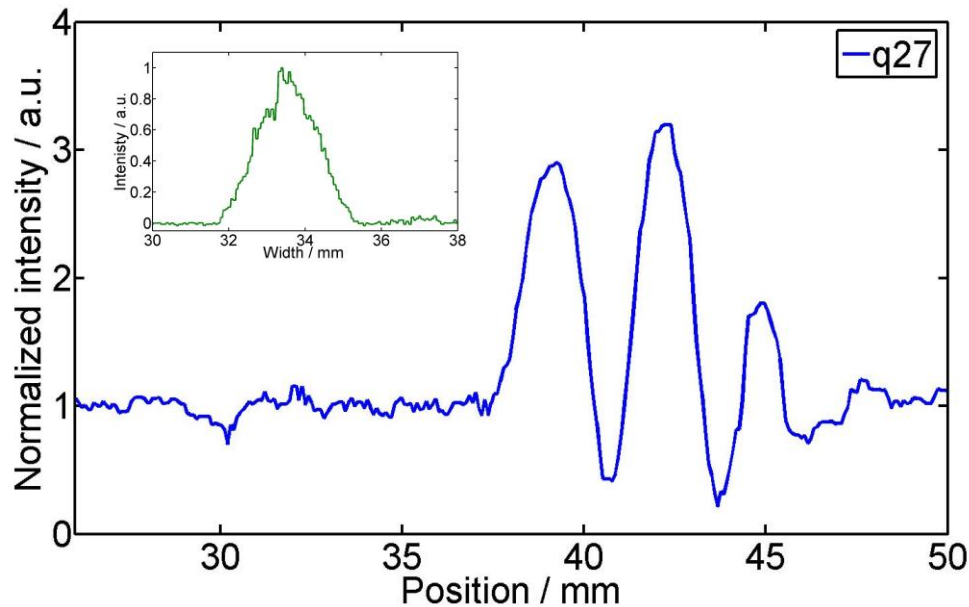


# Results for single CP pulse



- Oscillations give coherence length
- $L_c$  decreases with increasing harmonic order
- Maximum enhancement occurs when  $w = d = 2L_c$

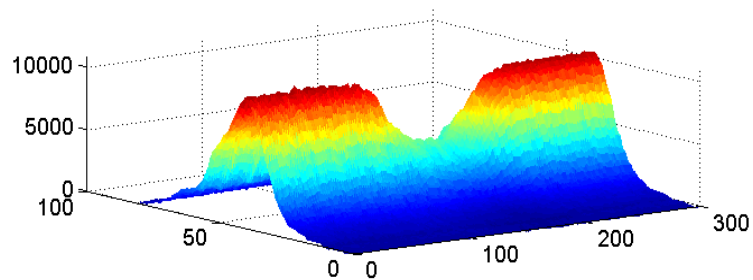
# Results for single CP pulse



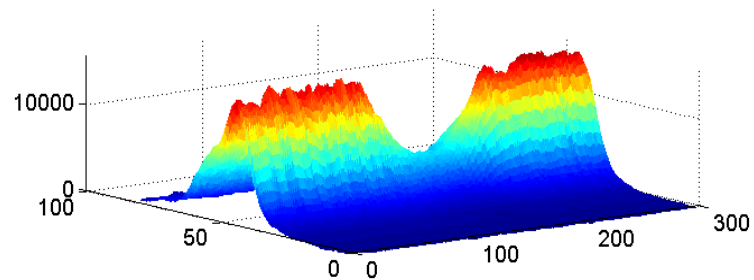
- Oscillations give coherence length
- $L_c$  decreases with increasing harmonic order
- Maximum enhancement occurs when  $w = d = 2L_c$

# HHG data

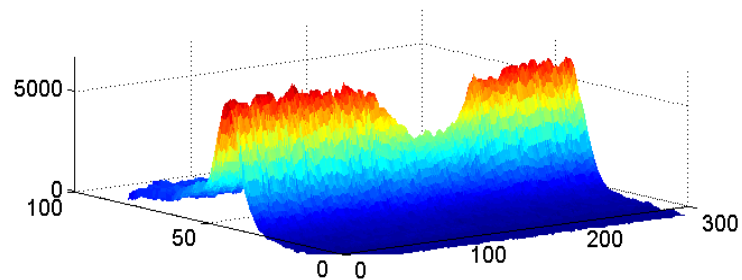
$q = 23$  Wedge = 21 mm



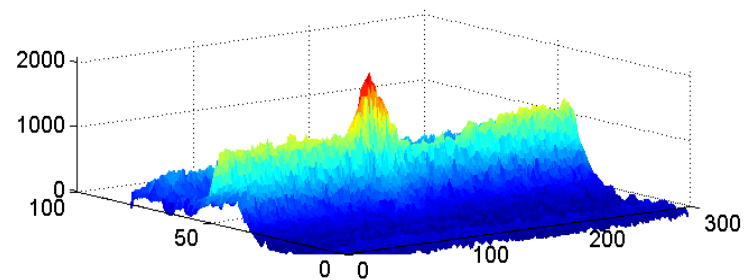
$q = 25$  Wedge = 21 mm



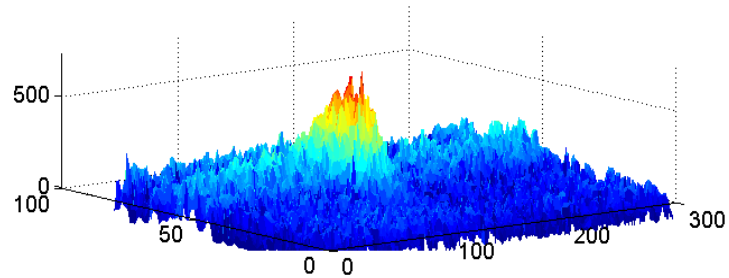
$q = 27$  Wedge = 21 mm



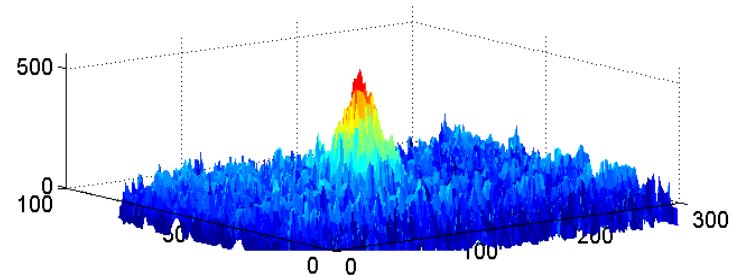
$q = 29$  Wedge = 21 mm



$q = 31$  Wedge = 21 mm

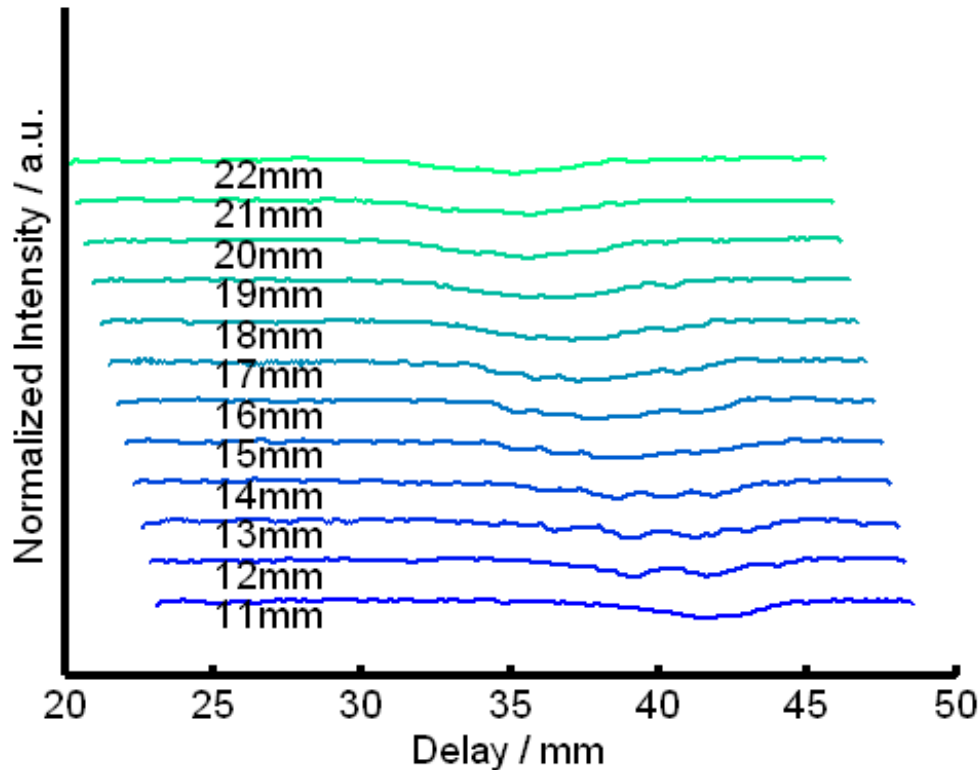


$q = 33$  Wedge = 21 mm



# HHG signal

$$q = 21$$



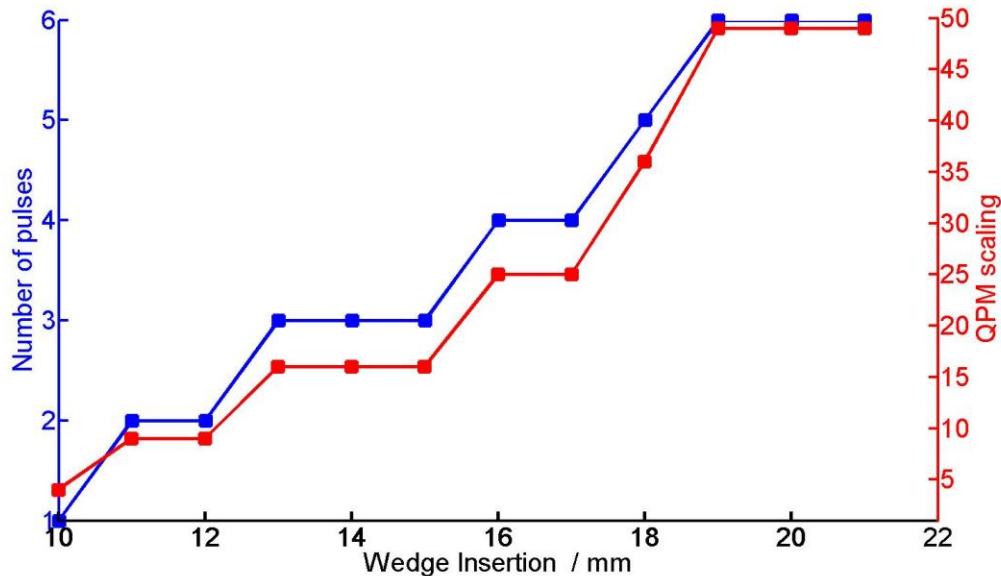
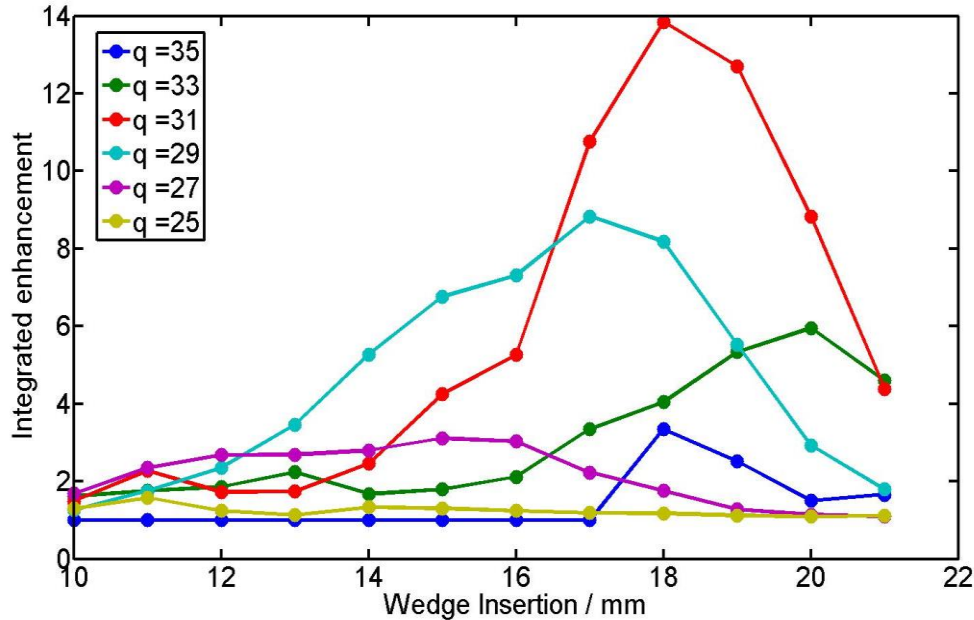
Low harmonic orders:

- suppression and coherent oscillations
- large pulse width

Higher harmonic orders:

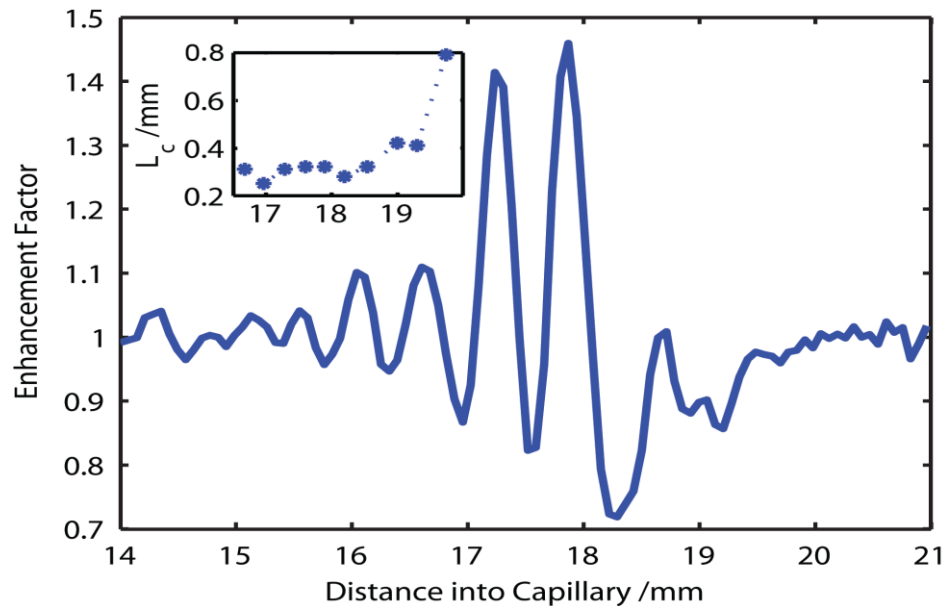
- enhanced signal due to QPM
- lower absorption
- more pulses in train
- enhancement until cutoff:  $q=35$

# Tunable enhancement



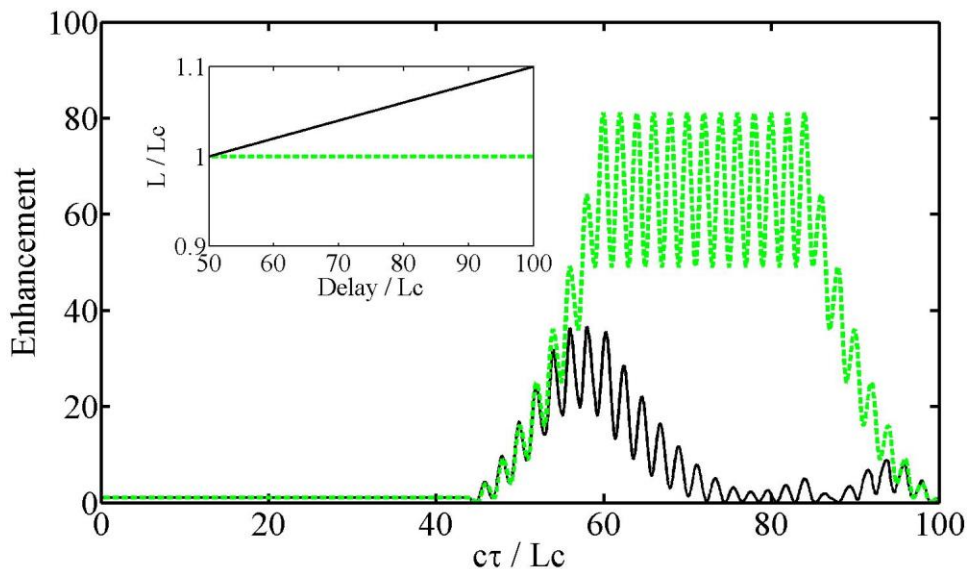
QPM intensity should  
scale as  $(N+1)^2$

# Variation of coherence length



Effects such as mode beating result in changes in the driver intensity

Coherence length varies as a function of position in the waveguide



Need to control coherence length, or have more tuneable pulse trains.

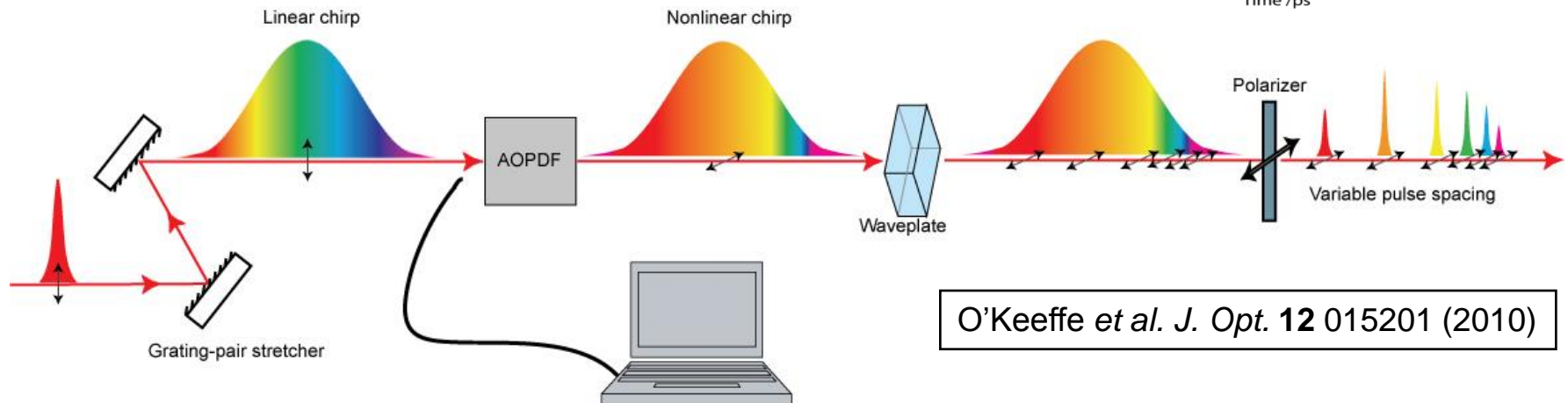
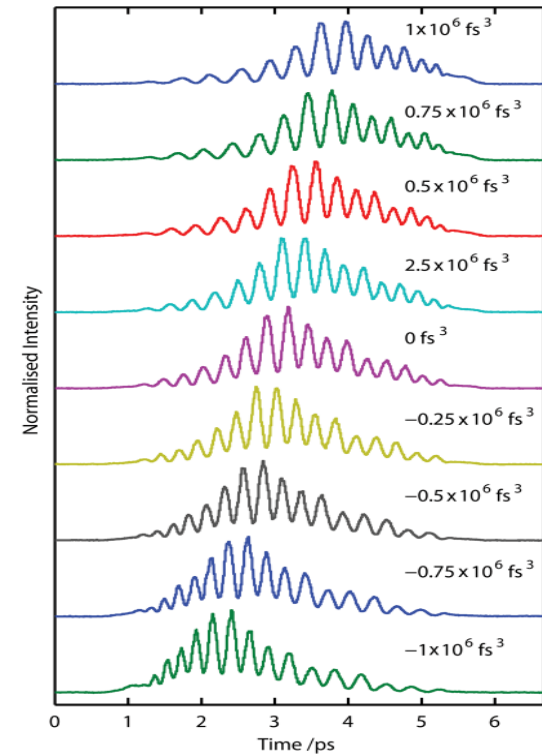
O'Keeffe *et al. Opt. Express.* **20** 6236, (2012)



# Adaptive pulse trains

- Transmitted frequencies are evenly spaced:  $\Delta\omega$ 
  - (neglecting GDD in wave plate and polarizer)
- Controlling dispersion controls when in stretched pulse transmitted frequencies occur
- Compensate for changing  $L_c$

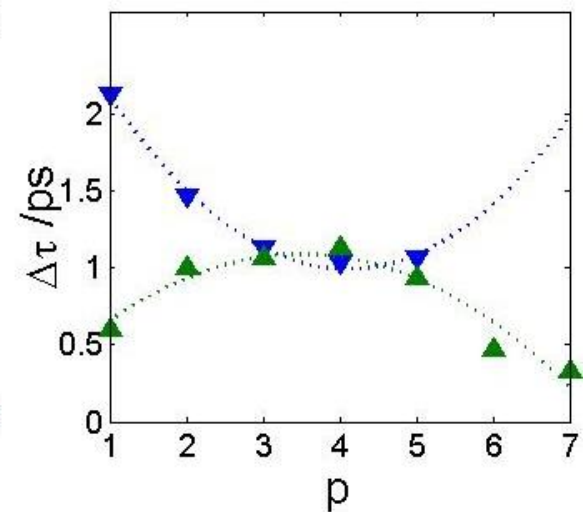
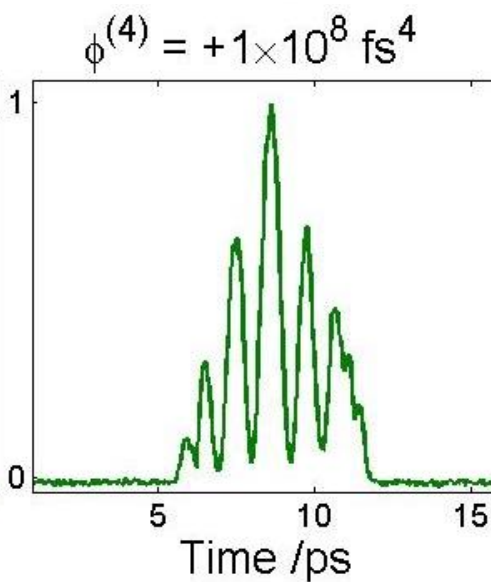
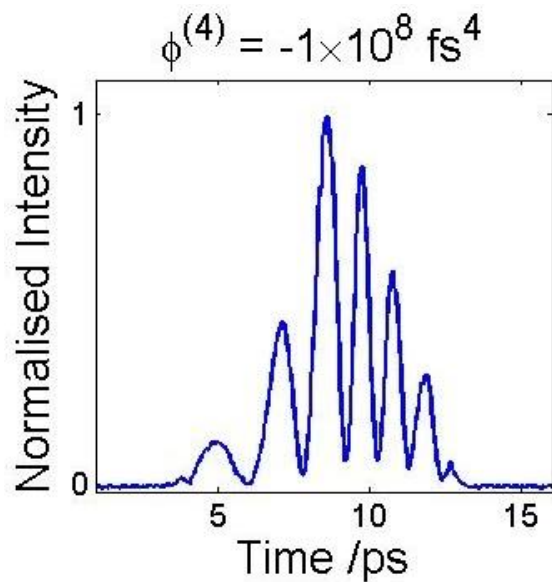
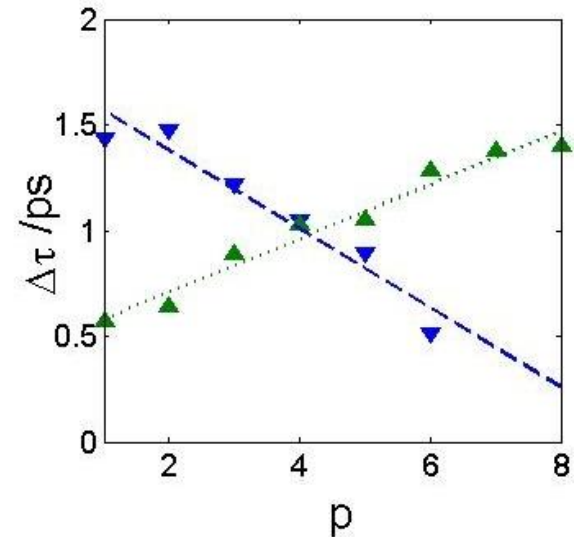
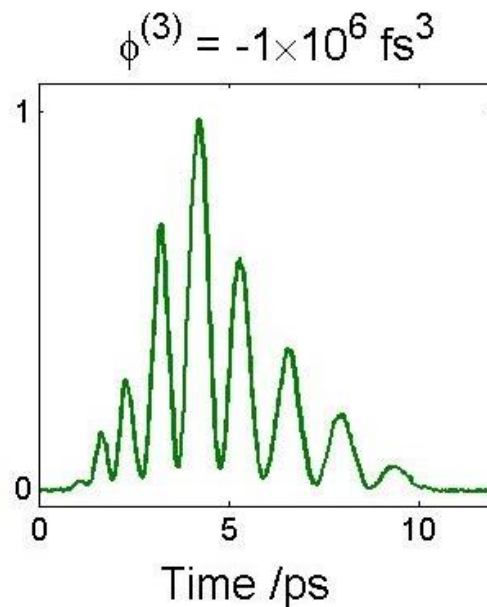
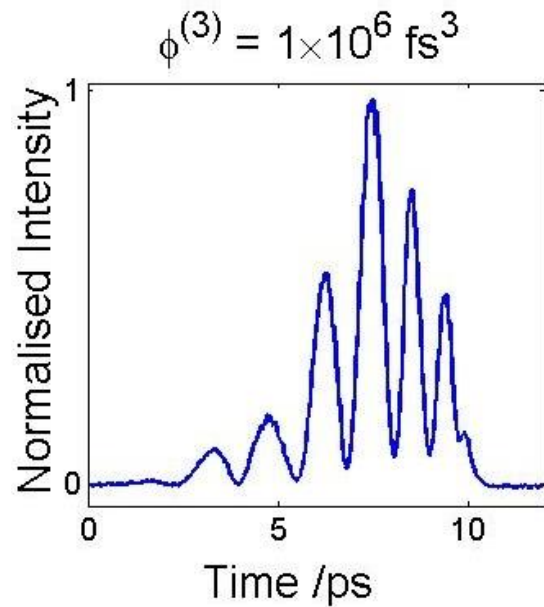
$$\Delta\tau_{p,p-1} \propto p^{n-2}$$



O'Keeffe *et al.* *J. Opt.* **12** 015201 (2010)

# Adaptive pulse trains

O'Keeffe *et al.* *J. Opt.* **12** 015201 (2010)



- Simple technique for generating flexible pulse trains
- Tunable quasi-phase-matched HHG
- Programmable pulse trains to compensate for varying  $L_c$

## **Future Work**

- Extend tunable QPM to high orders – shorter driving pulses
- EPSRC grant in collaboration with Engineering Department at Oxford
  - HHG to investigate particulate-strengthened alloys

# Thank you

**EPSRC** Engineering and Physical Sciences  
Research Council

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grant number EP/C005449

